

Masonry Beam Design

Strength Design Flexure and Shear

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Code References

- 2003 International Building Code (IBC)
- 2006 International Building Code (IBC)
- 2002 ACI 530/ASCE5/TMS402 by the Masonry Standards Joint Committee (MSJC)
- 2005 ACI 530/ASCE5/TMS402 by the Masonry Standards Joint Committee (MSJC)

Note:

** indicates equations found within general text books that are not contained in IBC , ASCE, or MSJC codes or commentaries.

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Code References for Beam Design

There are few changes between
the 2003 IBC/02 MSJC
and
the 2006 IBC /05 MSJC

Exceptions will be noted

Otherwise code references apply to either code

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Beam Strength Design

Beam Design Using Factored Loads and Strength Reduction Factors

- 2006 International Building Code (IBC)
(2006 IBC) Section 2108
- 2005 ACI 530/ASCE5/TMS402 by the Masonry Standards Joint Committee (MSJC)
(2005 MSJC) Chapter 3

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Beam Strength Design

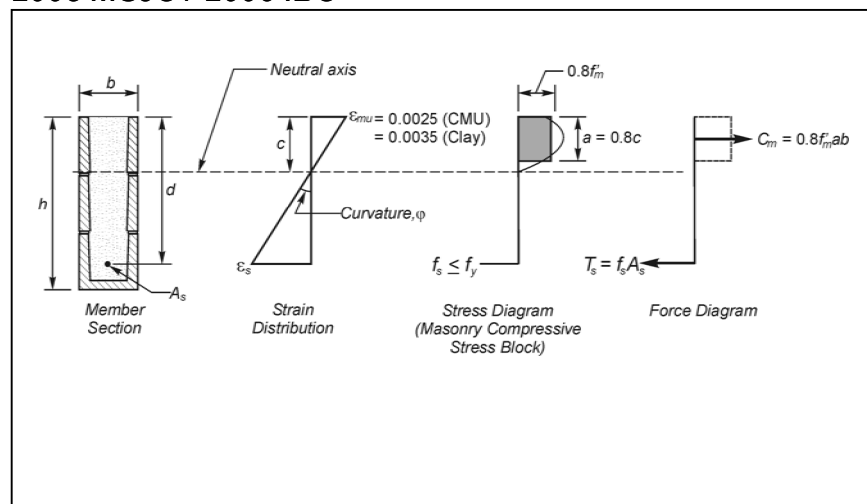
Masonry strength design is similar to concrete strength design using the Whitney Stress Block except that some assumptions are different

- Maximum Usable Strain
- Depth of Compression Block
- Average Stress on Compression Block

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Beam Strength Design

2005 MSJC / 2006 IBC



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Equilibrium of Beam Cross Section

$$C_m = .8 f'_m a b$$

a = depth of compression block

$$T_s = A_s F_y$$

$$T_s = C_m$$

$$A_s F_y = .8 f'_m a b$$

$$a = \frac{A_s f_y}{0.80 f'_m b}$$

$$M_n = (T)(jd) = A_s f_y \left(d - \frac{a}{2} \right)$$

$$M_u = \phi M_n$$

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Flexural Strength of Beam Cross Section

$$M_n = (T)(jd) = A_s f_y \left(d - \frac{a}{2} \right)$$

$$a = \frac{A_s f_y}{0.80 f'_m b}$$

$$M_u = \phi M_n$$

$$M_u = \phi A_s f_y \left(d - \frac{A_s f_y}{(2)(0.80) f'_m b} \right)$$

$$A_s = \rho b d$$

$$M_u = \phi \rho b d f_y \left(d - \frac{(\rho b d) f_y}{(2)(0.80) f'_m b} \right)$$

$$M_u = \phi \rho b d^2 f_y \left(1 - 0.63 \left(\rho \frac{f_y}{f'_m} \right) \right)$$

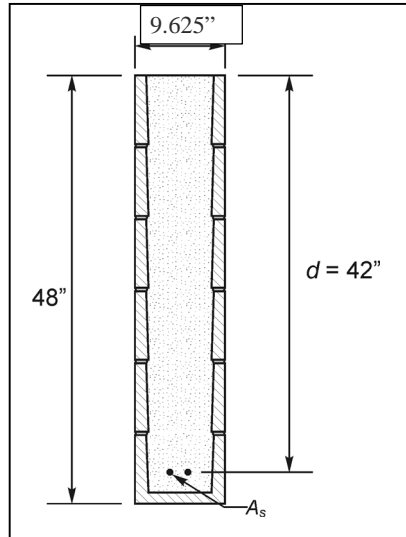
$$\text{Let } q = \rho \frac{f_y}{f'_m}$$

$$= \phi b d^2 f'_m q (1 - 0.63 q)$$

Solve for q to find required A_s

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Beam Design Example



- Beam is solid grouted 10 inch CMU
 - $L_{clear} = 8'-0"$
 - $M_u = 160$ kip-ft; $V_u = 80$ k
 - $f'_m = 2500$ psi
 - Grade 60 steel
 - Type S Mortar
- Determine required flexural reinforcement**

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Beam Design Example

Load Combinations

$$1.2D + 1.6L \quad \text{IBC 1605.2.1}$$

Flexural Strength Reduction Factor (No Axial Loads):

$$P=0 < 0.05A_n f'_m \quad \text{MSJC: 3.3.4.2.1}$$

$$\phi = 0.90 \quad \text{MSJC: 3.1.4.1}$$

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Beam Design Example

2005 MSJC:

$$M_u = \phi b d^2 f_m q (1 - 0.63q)$$

$$(160)(12) = (0.9)(9.63)(42)^2 (2.5) q (1 - 0.63q)$$

$$0.0502 = q(1 - 0.63q)$$

$$0.63q^2 - q + 0.0502 = 0$$

Solve quadratic equation

$$q = \frac{-(-1) \pm \sqrt{1 - 4 \cdot (0.63) \cdot (0.0502)}}{2 \cdot (0.63)} \quad q = 0.052$$

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Beam Design Example

2005 MSJC:

$$q = 0.052 \quad \rho = q \frac{f'_m}{f_y}$$

$$\rho = (0.052) \frac{2.5 \text{ ksi}}{60 \text{ ksi}} \quad \rho = 0.0022$$

$$A_s = \rho b d = 0.0022 (9.625 \text{ in}) (42 \text{ in})$$

$$A_s = 0.875 \text{ in}^2 \quad \text{Use 2-#6 } A_s \text{ actual} = 0.88 \text{ in}^2$$

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Beam Design Example

2005 MSJC:

Actual Nominal Flexural Capacity:

$$M_n = b d^2 f'_m q (1 - 0.63q) \quad q = [A_s / (bd)] (f_y / f'_m)$$

$$q = [(0.88 \text{ in}^2) / (9.625'')(42'')] (60 \text{ ksi} / 2.5 \text{ ksi}) = 0.0522$$

$$M_n = (9.625'') (42 \text{ in}^2) (2.5 \text{ ksi}) (0.0522) [1 - 0.63(0.0522)] (1' / 12'')$$

$$M_n = 179 \text{ k-ft (will need for upcoming check)}$$

$$\phi M_n = 0.9 * 179 \text{ k-ft} = 161 \text{ k-ft} > M_u = 160 \text{ k-ft}$$

Flexural Capacity OK
and efficient

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Check Beam Cracking Moment

2005 MSJC / 2006 IBC

MSJC Section 3.3.4.2.2.2 Minimum Capacity: $1.3M_{cr} \leq M_n$

Table 3.1.8.2.1:

tensile stress parallel to bed joints, fully grouted, Type S
mortar $f_r = 200 \text{ psi}$

$$1.3M_{cr} = 1.3S_x f_r$$

$$= 1.3 * [(9.625 \text{ in}) * (48 \text{ in})^2 / 6] * [(200 \text{ psi}) / [(12 \text{ in/ft}) * (1000 \text{ lb/k})]]$$

$$1.3M_{cr} = 1.3(61.60 \text{ ft-kip}) = 80 \text{ ft-kip} < M_n = 179 \text{ k-ft}$$

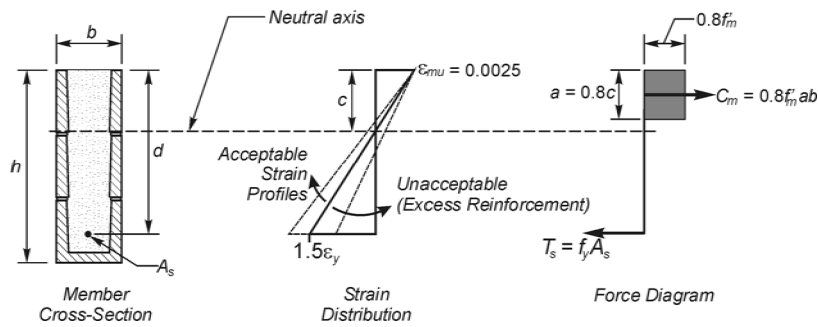
*Nominal Flexural Strength OK

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Check Maximum Reinforcement

2005 MSJC / 2006 IBC

Section 3.3.3.5.1:



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Check Maximum Reinforcement

2005 MSJC / 2006 IBC---changed from 2002 MSJC/2003 IBC

Section 3.3.3.5.1:

$$\rho_{\max} = \frac{A_{s,\max}}{bd} = 0.64 \frac{f'_m}{f_y} \left(\frac{\epsilon_{mu}}{\alpha\epsilon_y + \epsilon_{mu}} \right) \quad (\text{CC 3.3.3.5})$$

For concrete masonry beams with no axial load:

$$\alpha = 1.5$$

$$\epsilon_{mu} = 0.0025 \quad \text{for CMU} \quad (3.3.2.(c))$$

$$\rho_{\max} = 0.64 \left(\frac{2.5}{60} \right) \left(\frac{0.0025}{1.5(60)/29000 + 0.0025} \right) = 0.012$$

$$\rho = \frac{A_s}{bd} = \frac{0.88}{(9.5)(42)} = 0.0022 < \rho_{\max} = 0.012$$

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Beam Shear Strength

- Beam shear strength design is similar to concrete shear strength design.
- The total shear strength is based on combined masonry and steel contributions

$$V_n = V_m + V_s \quad \text{MSJC Equation (3-18)}$$

There is no guidance for evaluating the shear force location at a distance of $d/2$ away from the support (similar to Allowable Stress Design). Therefore, we take V_u at the face of support. (You may also reasonably chose to check at $d/2$ from support).

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Beam Shear Strength

2005 MSJC / 2006 IBC

▪ $\phi = 0.80$ MSJC 3.1.4.3

▪ SHEAR: Section 3.3.4.1.2

▪ $V_m = [4 - 1.75\{M/(Vd_v)\}]A_n(f'_m)^{1/2} + 0.25P$
where $M/(Vd_v) \leq 1.0$ Eqn (3-21)

For beams with no axial loads, $P = 0$

▪ $V_s = 0.5(A_v/s) f_y d_v$ Eqn (3-22)

▪ both equations are empirical and are research derived

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Beam Shear Strength

Total masonry shear strength is based on combined moment and shear components where M is the moment at the location that shear is checked.

$$V_m = [4 - 1.75\{M/(Vd_v)\}]A_n(f'_m)^{1/2}$$

If M & V due to a purely uniform load, at end of beam
M=0 @ V_{max} , therefore

$$M/Vd_v=0$$

If a centered concentrated load, $M=PL/4$ and $V=P/2$ at the centerline. $M/(V d_v) = 1/2(L/d_v)$ so longer spans reduce shear capacity.

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Beam Shear Strength

Example for the same beam problem:

- Span, $L_{clear} = 8'-0''$
- Axial Load, $P = 0$
- $V_u = 80$ kips
- $f'_m = 2500$ psi
- $f_y = 60$ ksi
- $b = 9.625$ in
- $d_v = h = 48$ in (MSJC 1.5)
- $A_n = b*d_v = 9.625'' * 48'' = 462$ in²

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Beam Shear Strength

- The 2005 MSJC 3.1.3 provides an overall ductility requirement for shear only. Specifics follow.
- The intent is to provide a ductile failure mechanism in flexure prior to a shear failure.
- The shear capacity must correspond to a loading that produces a moment that is 25% higher than the actual flexural capacity of the member but less than 2.5 times the calculated V_u .

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Beam Shear Strength

- MSJC ductile shear requirement will apply only to special reinforced shear walls, not beams, beginning in MSJC 2008 (1.17.3.2.6.1)
- Could defend that this corrected requirement should not apply to non tie-beam shear design (or any beam design) under the MSJC 2005 code.
- Both versions presented in the remainder of the example

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Beam Shear Strength

- MSJC 3.1.3: ΦV_n shall exceed the shear corresponding to 1.25 times the nominal flexural strength, $1.25M_n$, but need not exceed 2.5 times the required shear strength, $2.5V_u$. Call location of $1.25M_n$ the "ductile" location:
 - $M_{ductile} = 1.25M_n = 1.25(179 \text{ k-ft}) = 224 \text{ k-ft}$
 - $M = wL^2/8$ *uniform distributed loading
 - Solve for ductile w , $w = 8M/L^2$
 $= 8(224 \text{ ft-k})/(8 \text{ ft})^2 = 28 \text{ kips/ft}$
 - Corresponding $V_{ductile}$ at $1.25 M_n$
 $= wL/2 = (28 \text{ k/ft})(8 \text{ ft})/2 = 112 \text{ kips}$

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Beam Shear Strength

$V_{ductile}$ at $1.25 M_n$ loading = 112 kips
But need not exceed:

$V_{max} = 2.5V_u = 2.5(80 \text{ k}) = 200 \text{ k} > 112 \text{ k}$
Use $V_{max} = 112 \text{ k}$ controls

$\Phi V_{n \min} = 112 \text{ k} > V_u = 80 \text{ k}$

In future codes, this requirement will NOT apply to beams or other elements except special reinforced shear walls. The example will continue with both 80 kips and 112 kips for comparison. (The $V_{ductile}$ value will no longer be a beam shear parameter.)

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Beam Shear Strength

M=0 @ Max V and the shear strength of the masonry is then,

$$V_m = [4 - 1.75\{M/(Vd_v)\}]A_n(f'_m)^{1/2}$$

$$V_m = [4 - 0](462\text{in}^2)(2500\text{psi})^{1/2} + 0 = 92.4 \text{ kips}$$

$$\Phi V_m = (0.8)92.4\text{k} = 73.9 \text{ kips} < V_u = 112 \text{ k}, 80 \text{ k}$$

*MSJC 3.3.4.2.3 *Transverse reinforcement is Required (Stirrups)*

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Beam Shear Strength

- Check $A_{v \min}$:
 - MSJC 3.3.4.2.3(c):
 - (a) and (b) provide details for stirrups
 - $A_{v \min} = 0.0007bd_v = 0.0007(9.625\text{in})48\text{in} = 0.32 \text{ in}^2$
 - Use #5 bar -- Within 5% of $A_{v \min} = 0.32 \text{ in}^2$ and #6 bars are not practical for beam stirrups.
 - Could use #4, 2-leg for $A_v = 0.40 \text{ in}^2$ but difficult to position in a 10 inch wide beam

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Beam Shear Strength

- Calculate stirrup requirements
 - $V_u \leq \Phi(V_m + V_s)$
 $112 \text{ (80K) kips} \leq 0.8(92.4\text{k} + V_s)$
 Solve for V_s , $V_{u \text{ ductile}} = 112\text{k}$, $V_s = 47.6 \text{ kips}$
 $V_u = 80\text{k}$, $V_s = 7.60 \text{ kips}$
 - *MSJC 3.3.4.1.2.3: Eqn (3-22)*
 - $V_s = 0.5(A_v/s) f_y d_v$

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Beam Shear Strength

$$V_u = 112 \text{ k}, V_s \text{ ductile} = 47.6 \text{ kips}$$

$$V_u = 80 \text{ k}, V_s = 7.60 \text{ kips}$$

$$s = \frac{0.5A_v f_y d_v}{V_s} = \frac{0.5(0.31 \text{ in}^2)(60 \text{ ksi})(48 \text{ in})}{(47.6 \text{ kips})}$$

$$= 9.38 \text{ in} \longrightarrow \#5 \text{ at } 8 \text{ in (block module)}$$

actual V_s at 8"oc = 55.8 k

$$s = \frac{0.5A_v f_y d_v}{V_s} = \frac{0.5(0.31 \text{ in}^2)(60 \text{ ksi})(48 \text{ in})}{(7.60 \text{ kips})}$$

$$= 58.74 \text{ in} \longrightarrow \#5 \text{ at } d/2 = \underline{24 \text{ inch}} \text{ or } 48 \text{ inch}$$

max
actual V_s at 24"oc = 18.60 k

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Beam Shear Strength

where maximum spacing, S_{\max} , is from:

- MSJC 3.3.4.2.3(e):
- $S_{\max} = h/2 = (48 \text{ in})/2 = 24''$
- $S_{\max} = 48 \text{ in}$

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Beam Shear Strength

- Check actual Max V_n to preclude brittle failures:
 - MSJC 3.3.4.1.2 (a-c):
 - $(M_u/V_u d_v \leq 0.25)$: Eqn (3-19)
$$V_n \leq 6A_n [f'_m]^{1/2}$$
 - $(M_u/V_u d_v \leq 1.0)$: Eqn (3-20)
$$V_n \leq 4A_n [f'_m]^{1/2}$$
 - $V_{n\max}$ is permitted to be interpolated between the two values.

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Beam Shear Strength

$M_u=0$ @ Max V_u and thus $M_u/V_u d_v = 0$:

- Eqn 3-19: $V_{n \max} = 6A_n [f'_m]^{1/2}$
 $V_{n \max} = 6(462 \text{ in}^2)(2500 \text{ psi})^{1/2} = \underline{139 \text{ kips MAX}}$
- Eqn 3-18 $V_n = V_m + V_s$ or V_s ductile
 $V_n = 92.4 \text{ k} + 55.8 \text{ k} = 148.2 \text{ kips so } = 139 \text{ k max capacity}$

$\Phi V_n = 0.8(139 \text{ k}) = 111 \text{ k} \sim V_u \text{ ductile} = 112 \text{ k}$,
 But within 5%, Shear Strength OK for ductile requirement

- Eqn 3-18 $V_n = V_m + V_s$ or V_s ductile
 $V_n = 92.4 \text{ k} + 18.6 \text{ k} = 111.0 \text{ kips capacity} < 139 \text{ k}$
 $\Phi V_n = 0.8(111 \text{ k}) = 88.8 \text{ k} > V_u = 80 \text{ k}$, OK

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Beam Shear Strength

MSJC 3.3.4.2.3(d):

The first transverse bar shall be located within $d_v/4$ of the beam end.

$d_v/4 = 48''/4 = 12'' > s = 8''$ for block module

*Start first stirrup in first cell at 4 inches from the face of the opening to be centered in the first cell.

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Beam Shear Strength

The spacing of the stirrups can be increased for the locations farther away from the support as actual shear decreases - similar to allowable stress design or concrete strength design.

Although shear reinforcing is not required by code for some locations in the beam where $V_u \leq \Phi V_{m,r}$ in higher seismic areas, it is good practice to use min $d_v/2$ (or at least d_v) spaced shear reinforcing throughout the beam length for ductility purposes.